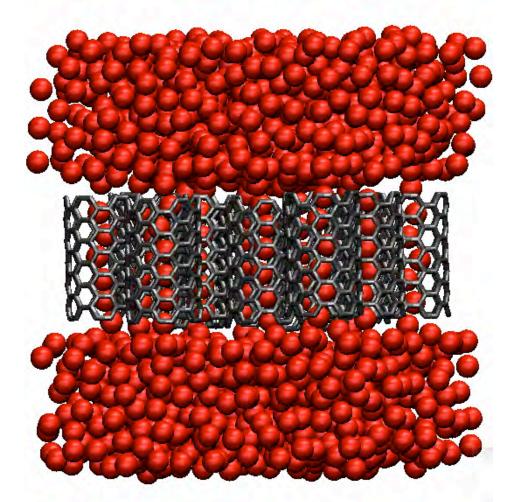
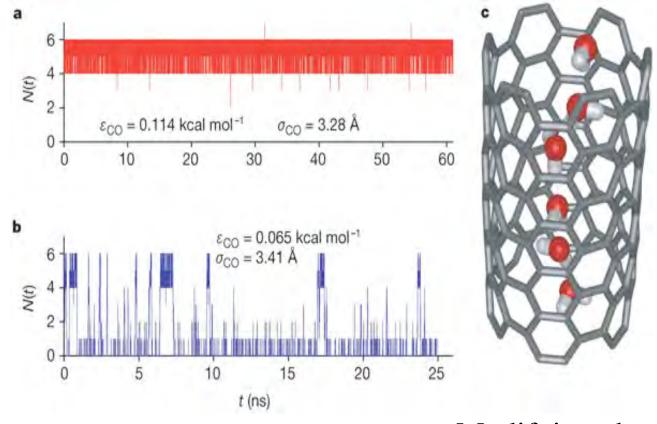
Carbon Nanotubes Hydrophobic channels - Perfect Models for Membrane Water Channels



A balance between the size and hydrophobicity

Water-nanotube interaction can be easily modified



Modifying charges Modifying vdW parameters

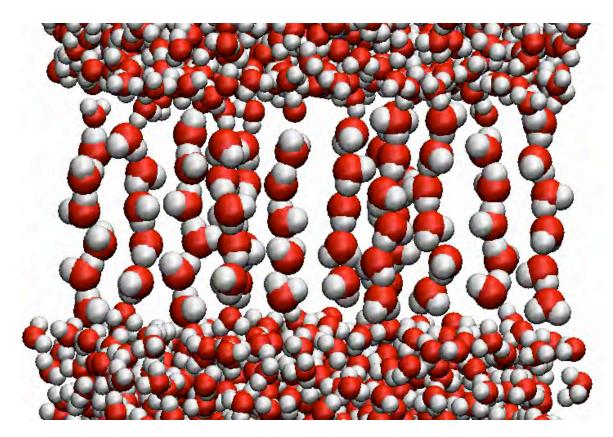
Hummer, et. al., Nature, 414: 188-190, 2001

Carbon Nanotubes Hydrophobic channels - Perfect Models for Membrane Water Channels



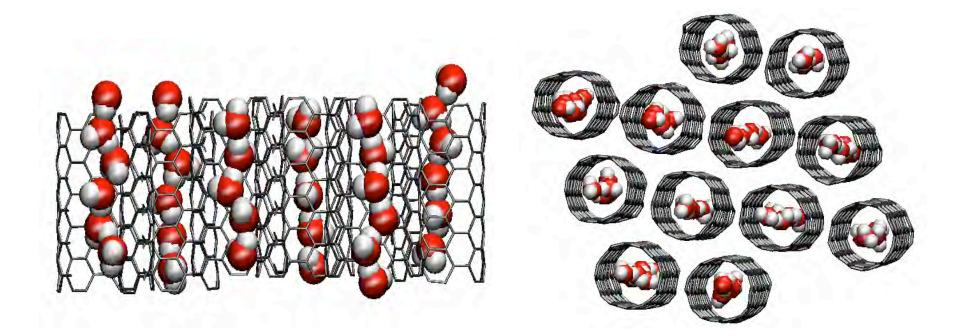
- Much better statistics
- No need for membrane and lipid molecules

Carbon Nanotubes Hydrophobic channels - Perfect Models for Membrane Water Channels



- Much better statistics
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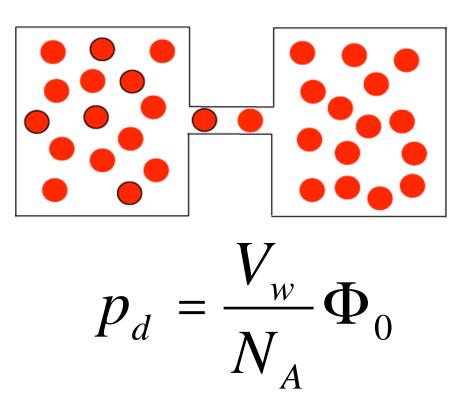
Water Single-files in Carbon Nanotubes



Water files form polarized chains in nanotubes

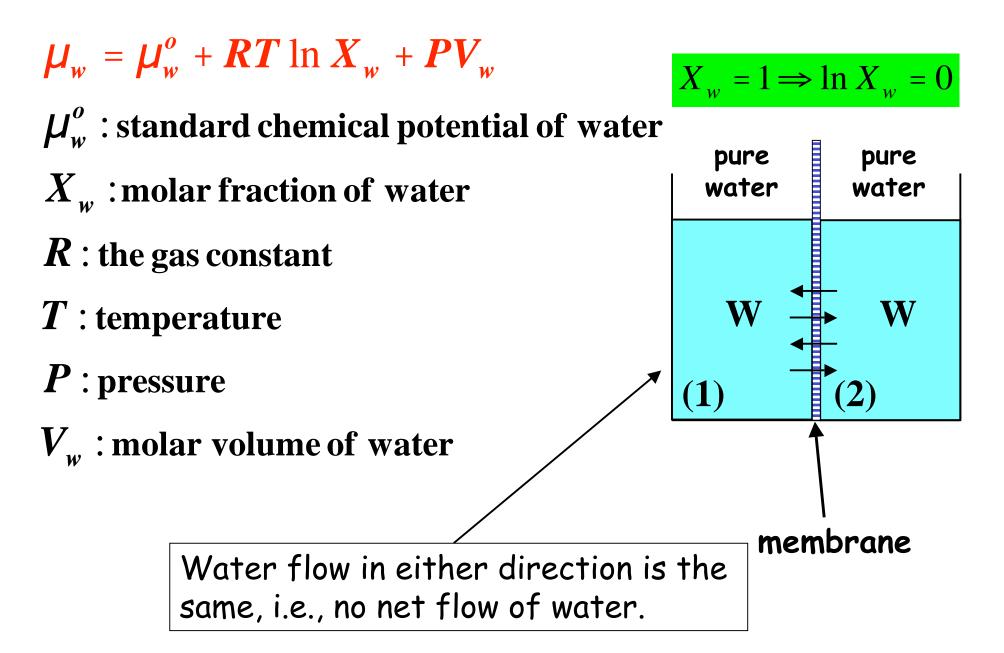
Calculation of Diffusion Permeability from MD

 Φ_0 : number of water molecules crossing the channel from the left to the right in unit time



 Φ_0 can be directly obtained through equilibrium MD simulation by counting "full permeation events"

Chemical Potential of Water



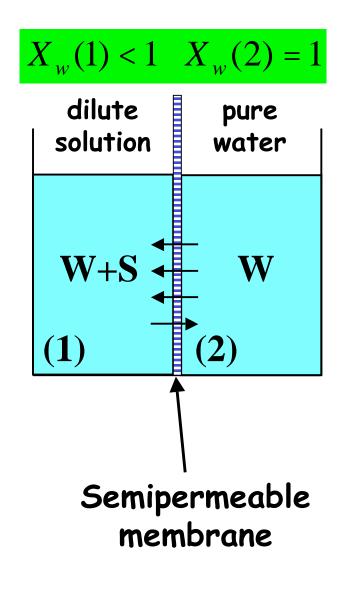
Solutes Decrease the Chemical Potential of Water

$$\mu_w = \mu_w^o + RT \ln X_w + PV_w$$

Addition of an impermeable solute to one compartment drives the system out of equilibrium.

$$RT \ln X_w(1) < RT \ln X_w(2)$$
$$\Rightarrow \mu_w(1) < \mu_w(2)$$

Water establishes a net flow from compartment (2) to compartment (1).



Establishment of Osmotic Equilibrium

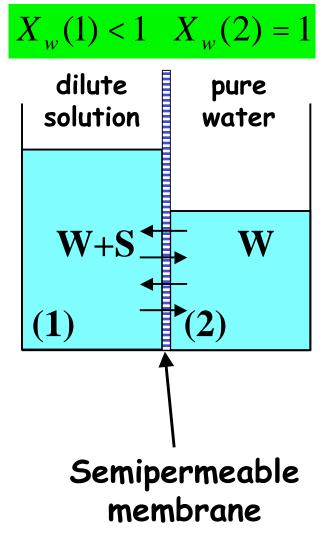
@equilibrium :
$$\mu_w(1) = \mu_w(2)$$

At equilibrium, the chemical potential of any species is the same at every point in the system to which it has access.

$$\mu_{w}^{o}(1) + RT \ln X_{w}(1) + P(1)V_{w} = \mu_{w}^{o}(2) + RT \ln X_{w}(2) + P(2)V_{w}$$

 $RT \ln X_w(1) + P(1)V_w = P(2)V_w$

 $\Delta PV_{w} = -RT \ln X_{w}(1)$



Establishment of an Osmotic Equilibrium $\Delta PV_{w} = -RT \ln X_{w}(1)$

 $X_w(1) < 1 \quad X_w(2) = 1$

pure

water

W

dilute

solution

W+S

(1)

Solute molar fraction in physiological (dilute) solutions is much smaller than water molar fraction.

$$X_{w} + X_{s} = 1 ; X_{s} << 1$$
$$\implies \ln X_{w} = \ln(1 - X_{s}) \cong -X_{s}$$

$$\Delta PV_{w} = RTX_{s}$$

$$\Rightarrow \prod = \Delta P = \frac{RT}{V_{w}}X_{s}$$
Osmotic pressure
Semipermeable membrane

Establishment of an Osmotic Equilibrium

$$\prod = \Delta P = \frac{RT}{V_w} X_s$$

Solute concentration (~0.1M) in physiological (dilute) solutions is much smaller than water concentration

on (55M).

$$n_s << n_w$$
(1)

E

 $X_{w}(1) < 1 \quad X_{w}(2) = 1$

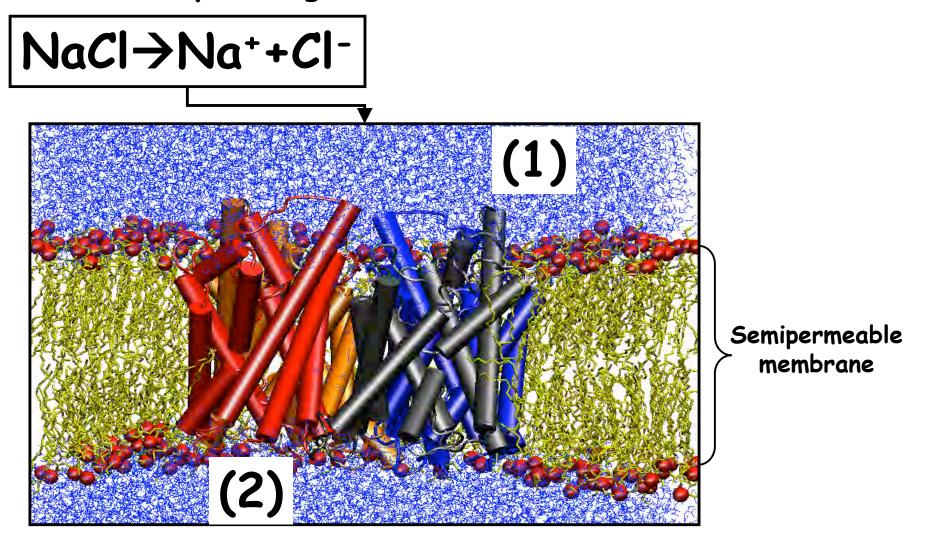
$$=\frac{n_s}{V_{tot}}V_w = C_s V_w$$

 $X_{s} = \frac{n_{s}}{n_{s} + n_{w}} \approx \frac{n_{s}}{n_{w}} = \frac{n_{s}}{n_{w}} \frac{V_{w}}{V_{w}}$

$$\Pi = \Delta \boldsymbol{P} = \frac{\boldsymbol{R}\boldsymbol{T}}{\boldsymbol{V}_{w}}\boldsymbol{C}_{s}\boldsymbol{V}_{w} = \boldsymbol{R}\boldsymbol{T}\boldsymbol{C}_{s}$$

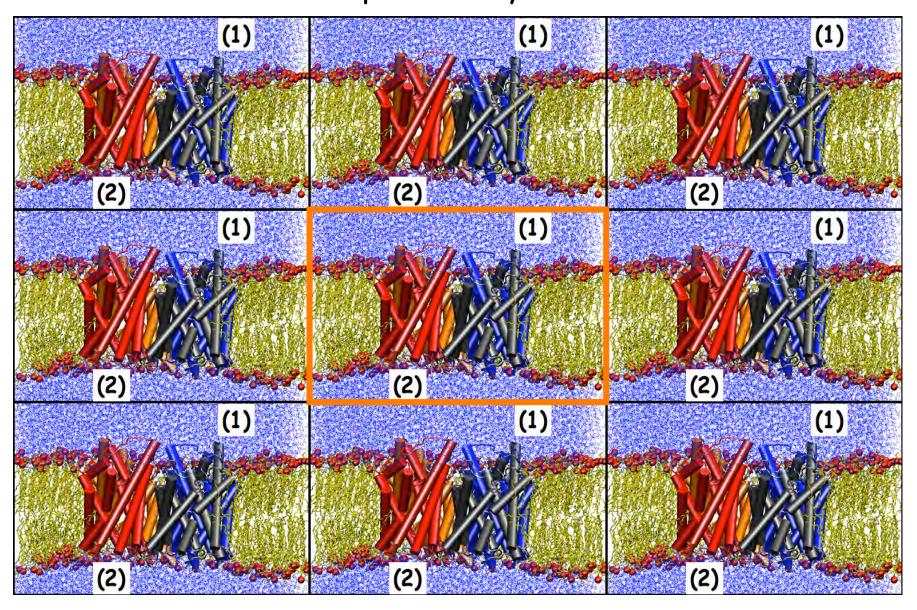
$$\Delta \Pi = \Delta P = RT \Delta C_s$$

Simulation of osmotic pressure induced water transport may be done by adding salt to one side of the membrane.

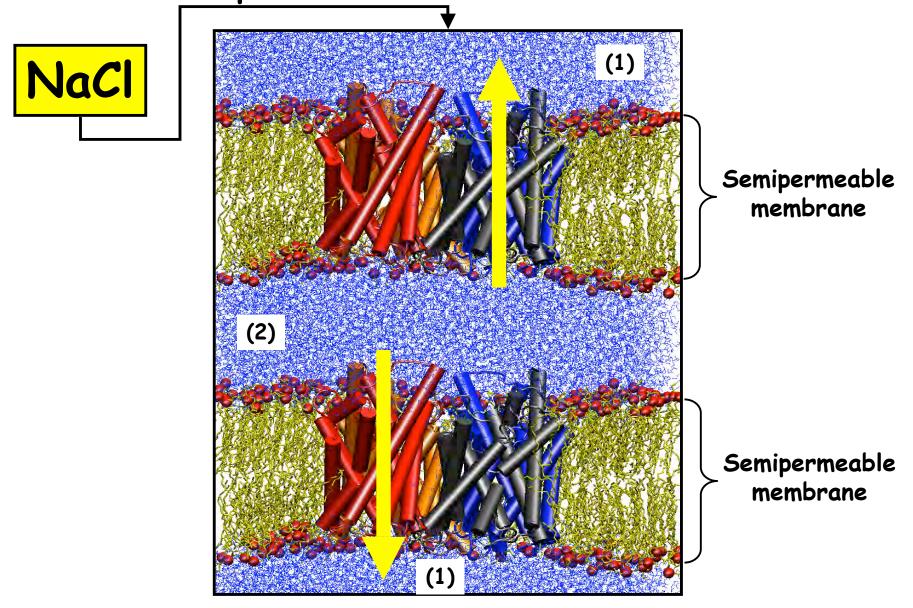


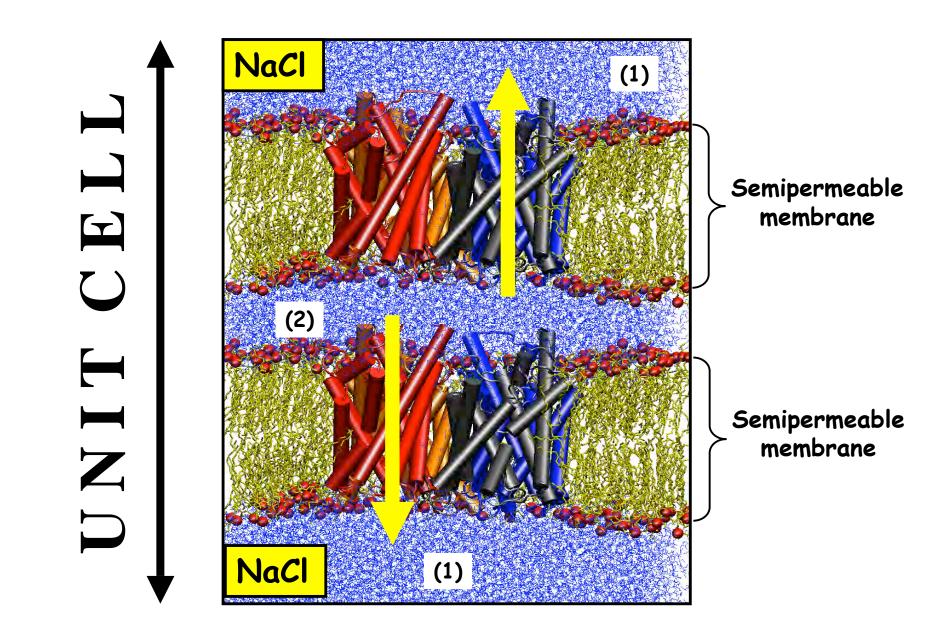
There is a small problem with this setup!

Problem: The solvents on the two sides of a membrane in a conventional periodic system are connected.



We can include more layers of membrane and water to create two compartment of water that are not in contact

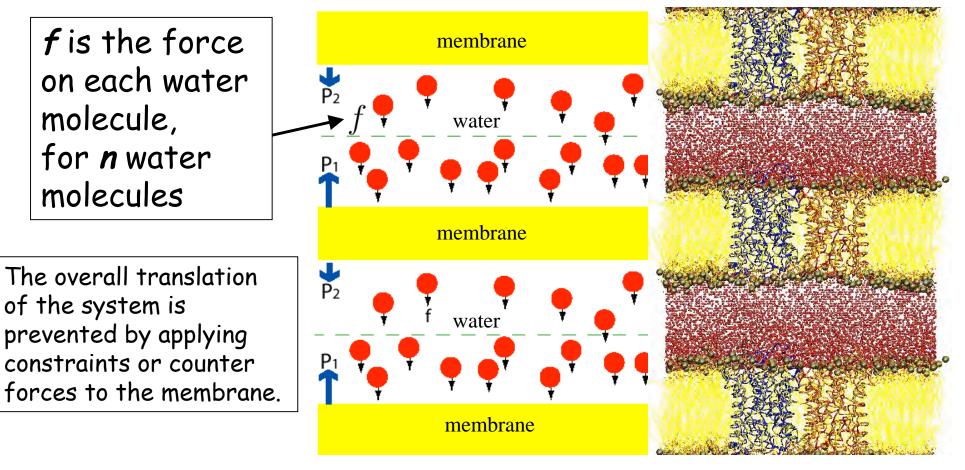




Realizing a Pressure Difference in a Periodic System

 $P_1 = P_2 + nf \Rightarrow \Delta P = nf / A$

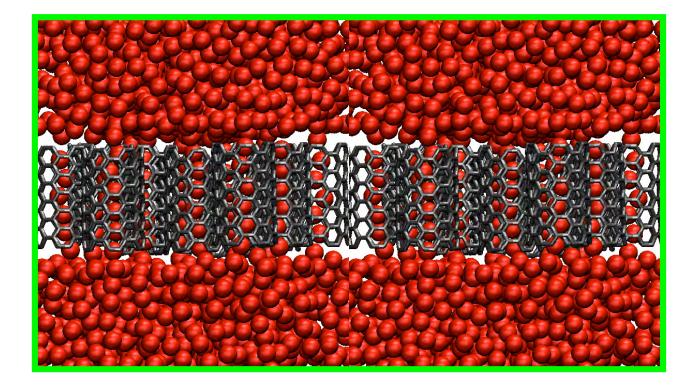
Fangqiang Zhu



F. Zhu, et al., Biophys. J. 83, 154 (2002).

Applying a Pressure Difference Across the Membrane

 $\Delta P = nf / A$

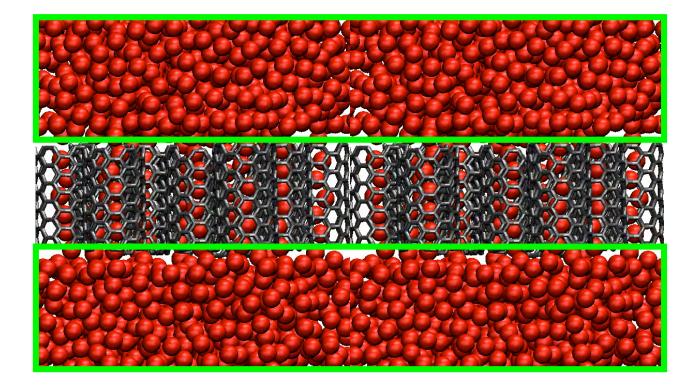


Applying force on all water molecules.

Not a good idea!

Applying a Pressure Difference Across the Membrane

 $\Delta P = nf / A$

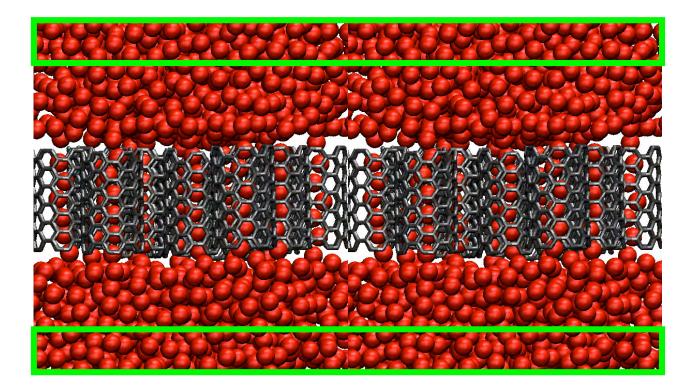


Applying force on bulk water only.

Very good

Applying a Pressure Difference Across the Membrane

 $\Delta P = nf / A$



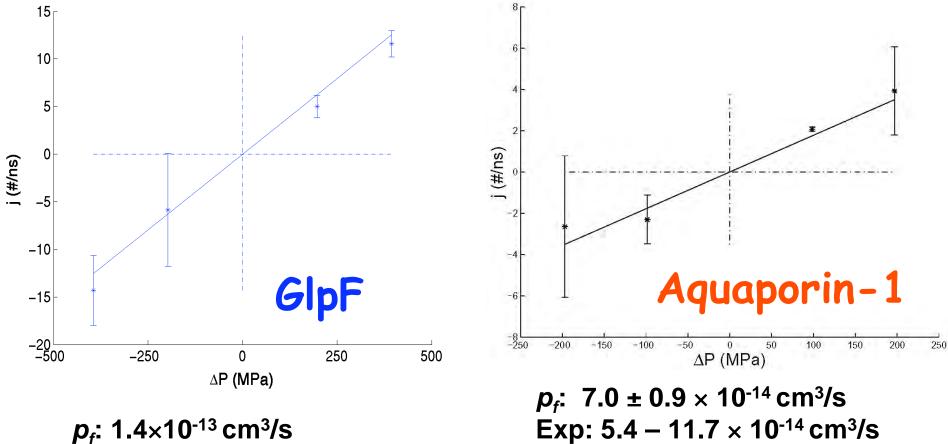
Applying force only on a slab of water in bulk.

Excellent

 P_f can be calculated from these simulations

$$\Phi_w = P_f A(\frac{\Delta P}{RT} - \Delta C_s)$$

Calculation of osmotic permeability of water channels



 p_{f} : 1.4×10⁻¹³ cm³/s



