NAMD Tutorial (Part 2)

2 Analysis

- > 2.1 Equilibrium
 - > 2.1.1 RMSD for individual residues
 - > 2.1.2 Maxwell-Boltzmann Distribution
 - > 2.1.3 Energies
 - 2.1.4 Temperature distribution
 - > 2.1.5 Specific Heat
- 2.2 Non-equilibrium properties of protein
 2.2.1 Heat Diffusion
 - > 2.2.2 Temperature echoes

Organization of NAMD Tutorial Files



Simulated Cooling of Ubiquitin

- Proteins function in a narrow (physiological) temperature range. What happens to them when the temperature of their surrounding changes significantly (temperature gradient) ?
- Can the heating/cooling process of a protein be simulated by molecular dynamics ? If yes, then how?



What can we learn from the simulated cooling/heating of a protein ?

Nonequilibrium (Transport) Properties

- macromolecular properties of proteins, which are related to their biological functions, often can be probed by studying the response of the system to an external perturbation, such as *thermal gradient*
- "small" perturbations are described by linear response theory (LRT), which relates transport (nonequilibrium) to thermodynamic (equilibrium) properties
- on a "mesoscopic" scale a globular protein can be regarded as a continuous medium \Rightarrow within LRT, the local temperature distribution T(r,t) in the protein is governed by the heat diffusion (conduction) equation

$$\frac{\partial T(\mathbf{r},t)}{\partial t} = D \nabla^2 T(\mathbf{r},t)$$



VS

Mesoscopic



- each atom is treated individually
- length scale ~ 0.1 Å
- time scale ~ 1 fs



- one partitions the protein in small volume elements and average over the contained atoms
- length scale ≥ 10 Å = 1nm
- time scale ≥ 1 ps





How to simulate cooling ?

- In laboratory, the protein is immersed in a coolant and the temperature decreases from the surface to the center
- Cooling methods in MD simulations:
 - 1. Stochastic boundary method
 - 2. Velocity rescaling (rapid cooling, biased velocity autocorrelation)

$$\langle T(t) \rangle_{sim} = \frac{\sum_{i=1}^{N_d} m_i v_i^2}{N_d k_B} \implies v_i' = v_i \sqrt{\frac{T_{new}}{T_{old}}}$$

3. Random reassignment of atomic velocities according to Maxwell's distribution for desired temperature (velocity autocorrelation completely lost)

Stochastic Boundary Method

Heat transfer through mechanical coupling between atoms in the two regions



coolant layer of atoms

motion of atoms is subject to stochastic Langevin dynamics $m \ddot{r} = F_{FF} + F_H + F_f + F_L$

 $F_{FF} \rightarrow$ force field $F_{H} \rightarrow$ harmonic restrain $F_{f} \rightarrow$ friction $F_{L} \rightarrow$ Langevin force

atoms in the inner region follow Newtonian dynamics

$$m \, \ddot{r} = F_{FF}$$



Thermal Conductivity of UBQ

 $K = D\rho c$

$$C_{V} = \langle \delta E^{2} \rangle / k_{B} T^{2} = \left(\langle E^{2} \rangle - \langle E \rangle^{2} \right) / k_{B} T^{2}$$

 $D \approx 0.97 \times 10^{-3} \ cm^2/s$ $\rho \approx 1 \times 10^3 \ kg/m^3$